Permutation and Combination Questions with Solutions Pdf

- 1. In how many different ways can the letters of the word AWARE be arranged?
- a. 40
- b. 60
- c. 120
- d. 150 -→

Ans:

The given word contains 5 letters of which A is taken 2 times.

∴ Required number of ways =
$$\frac{5}{2} = \frac{5 \times 4 \times 3 \times 2 \times 1}{2} = 60$$
.

- 2. In how many different ways can the letters of the word WEDDING be arranged?
- a. 2500
- b. 2520
- c. 5000
- d. 5040 -→

Ans:

The given word contains 7 letters of which D is taken 2 times.

.. Required number of ways

$$= \frac{\underline{|7|}}{\underline{|2|}} = \frac{7 \times 6 \times 5 \times 4 \times 3 \times 2 \times 1}{2 \times 1} = 2520.$$

- 3. In how many ways can a group of 5 men and 2 women be made out of a total of 7 men and 3 women?
- a. 45
- b. 63
- c. 90
- d. 126 -→

Required no. of ways

=
$$({}^{7}C_{5} \times {}^{3}C_{2}) = ({}^{7}C_{2} \times {}^{3}C_{1}) = \frac{7 \times 6}{2 \times 1} \times 3 = 63.$$

- 4. Out of 5 women and 4 men, a committee of three members is to be formed in such a way that at least one member is a woman. In how many different ways can it be done?
- a. 76
- b. 80
- c. 84
- d. 96 -→

Ans:

Required number of ways =
$$({}^{5}C_{1} \times {}^{4}C_{2}) + ({}^{5}C_{2} \times {}^{4}C_{1}) + ({}^{5}C_{3})$$

= $\left(5 \times \frac{4 \times 3}{2 \times 1}\right) + \left(\frac{5 \times 4}{2 \times 1} \times 4\right) + \left(\frac{5 \times 4 \times 3}{3 \times 2 \times 1}\right)$
= $(30 + 40 + 10) = 80$.

- 5. A committee of 5 members is to be formed out of 3 trainees, 4 professors and 6 research associates. In how many different ways can this be done, if the committee should have 4 professors and 1 research associate or all 3 trainees and 2 professors?
- a. 12
- b. 13
- c. 24
- d. 52 -→

Ans:

Required number of ways =
$$({}^{4}C_{4} \times {}^{6}C_{1}) + ({}^{3}C_{3} \times {}^{4}C_{2})$$

= $(1+6) + \left(1 + \frac{4 \times 3}{2}\right) = (7+7) = 14$.